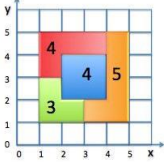
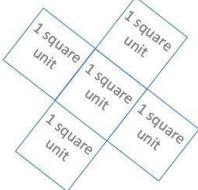
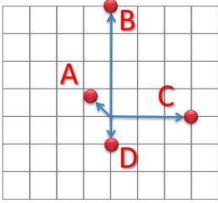
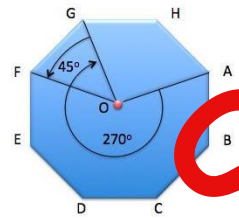



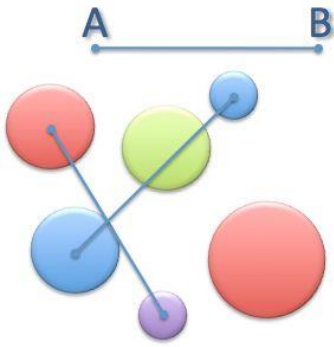
# Mathematical Reasoning 1

Question No.	Explanation
1	In this addition series, 1 is added to the first number; 2 is added to the second number; 3 is added to the third number; 4 is added to the fourth number; and go on.
2	Let the three integers be $x$ , $x + 2$ and $x + 4$ . Then, $3x = 2(x + 4) + 3x = 11$ . Third integer = $x + 4 = 15$ .
3	Average of 20 numbers = 0. Sum of 20 numbers ( $0 \times 20$ ) = 0. It is quite possible that 19 of these numbers may be positive and if their sum is $a$ then 20th number is $(-a)$ .
4	$3 \times 4 \times 5 = 60$
5	There are $8 \times 36 = 288$ stairs
6	$C / B = 0.75 / 0.5 = 0.75 \times 2 = 1.5$ (F)
7	$5.4 - 0.002 = 5.398$
8	Liquid: $1$ or $15/15$ Frozen: $15/15 + 1/15 = 16/15$ Liquid: $(1/15) / (16/15) = 1/16$
9	<p>Cancel adjacent numerators and denominators:</p> $\frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \dots \times \frac{124}{125} = \frac{1}{125} \times \frac{8}{1000} = 0.008$
10	$1 / 5$ jar = 24 candies. 1 jar = $5 \times 24 = 120$ candies. $1/2$ jar = $120/2 = 60$ candies.
11	The perimeter is the same as that of a $20 \times 30$ rectangle, which is $30 + 30 + 20 + 20 = 100$ .
12	<p>The red and blue shapes have the same area of 4 square units.</p> 
14	<p>The square side is 1 unit. <math>4 \times 3 = 12</math></p> 
15	A: 10 square units; B : 11 square units; C: 10 square units; D: 10 square units.

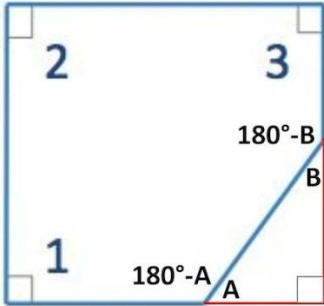
16	 <p style="color: red; text-align: center;"><math>AD &lt; CD &lt; AB &lt; BC</math></p>
17	Each train travels three times in 24 hours. $24/3 = 8$ trains
18	The dog ran 20 km because the speed was 20 km per 1 hour.
19.	Pipe 1 is as efficient as 2 of Pipe 2. Both Pipes 1 and 2 are efficient as 3 of Pipe 2. It takes 3 times less time for both pipes to empty the tank together than for Pipe 2. Two hours divided by 3 is equal to $2/3$ hours = $2 \times 60$ minutes / 3 = 40 minutes.
20	60 drops every minute. 3600 drops every hour. $3600/3000 \times 200$ ml = $6/5 \times 200$ ml = 240 ml every hour. $240 \times 24 = 5760$ ml = about 6 liters.
21	$123 - 12.5 + 45 - 125 = 123 + 45 - 125 - 12.5 = 168 - 125 - 12.5 = 43 - 12.5 = 30.5$
22	$650 - 120 + 540 - 230 + 430 - 340 = 530 + 310 + 90 = \$930$
23	Each separate digit costs \$10, "100" consists of three digits. $3 \times \$10 = \$30$
24	$\begin{aligned} A + 2 &= X & (1) \\ B + 3 &= X & (2) \\ A + B &< X & (3) \\ B > 0 & & (4) \end{aligned}$ <p>From (2) and (4), <math>X &gt; 3</math>  (1) + (2) gives <math>A + B = 2X - 5 &lt; X</math> using (3)  <math>X - 5 &lt; 0</math> giving <math>X &lt; 5</math>  but we know <math>X &gt; 3</math>, meaning <math>X = 4</math>.</p> <p><math>A = 2, B = 1, X = 4</math>.</p>
25	Flash Harry's bank balance looked like this. April – \$100 May + \$100 June – \$200 July + \$200 So Harry made \$200 overall.
26	1st day = 198 2nd day = $198 + 24 = 222$ 3rd day = $222 - 12 = 210$ 4th day = $210 + 29 = 239$ 4 day total = $198 + 222 + 210 + 239 = 869$
27	$(1 - 0.95) \times 5$ kg = 0.25kg (the slice weight without water). Let W = the new weight; then $0.25 / W = (1 - 0.75)$ $W = 0.25 / 0.25 = 1$ kg
28	$5 \times 0.85 + 3 \times 0.25 = 4.25 + 0.75 = 5$ kg. $5+3=8$
29	$10+8+8+8+8+8+8+8=10+56=66$

<p>30</p>	<p>56/14=4 98/14=7</p> <p>To solve this problem we first split each number down into its prime factors.</p> <p>There is only one possible way to write a number in terms of its prime factors (apart from the order in which they are written).</p> <p>56=2x2x2x7 98=2x7x7</p> <p>Now we notice that 2 and 7 are common prime factors, so <math>2 \times 7 = 14</math> is the largest possible common factor.</p>
<p>31</p>	<p>Let the ten's digit be x and unit's digit be y. Then, <math>(10x + y) - (10y + x) = 36</math> <math>9(x - y) = 36</math> <math>x - y = 4.</math></p>
<p>32</p>	<p>The pattern is <math>x \times 2, x \times \frac{3}{2}, x \times 2, x \times \frac{3}{2}, x \times 2, \dots</math> So, missing term = <math>1 \times \frac{3}{2} = \frac{3}{2}</math>.</p>
<p>33</p>	<p>The pattern is <math>+ 5, - 2, + 5, - 2, \dots</math> So, missing term = <math>36 - 2 = 34</math>.</p>
<p>34</p>	<p>The correct answer is 5 because the numbers are a Fibonacci sequence. This means that each number is the sum of the two numbers to its left. So, <math>2 + 3 = 5</math>.</p>
<p>35</p>	<p>The correct answer is 85 because the numbers are going down by 27 each time. 27 is the cube of the number 3: <math>3 \times 3 \times 3 = 27</math></p>
<p>36</p>	<p>The angle AOB is <math>360 / 8 = 45^\circ</math>.</p> 
<p>37</p>	<p>The triangle has two equal sides and is therefore isosceles. It therefore has two equal angles. We also use the rule that the sum of angles in any triangle is <math>180^\circ</math>.</p> <p><math>x + x + 55^\circ = 130^\circ</math> <math>2x = 125^\circ</math> <math>x = 62.5^\circ</math></p>
<p>38</p>	

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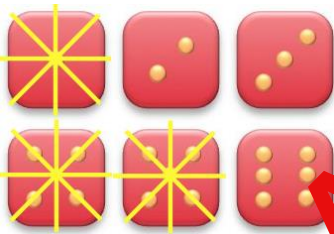


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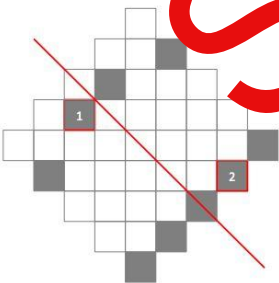


In the triangle,  $A+B+90^\circ=180^\circ$   
 $A+B=90^\circ$   
 Required angle is  $(180^\circ-A)+(180^\circ-B)=$   
 $360^\circ-(A+B)=360^\circ-90^\circ=270^\circ$

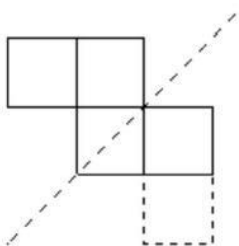
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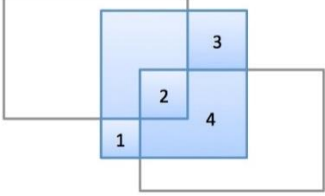
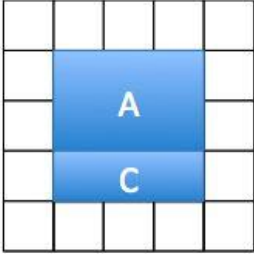


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45	The cube consists of $4 + 4 + 4 = 12$ matches. The roof consists of 5 matches. The door consists of 3 matches. $12 + 5 + 3 = 20$ matches.
46	
47	$6 \times 4 = 24$
49	You can make six different numbers. In order, the numbers are: 799, 899, 898, 979, 988, 997.
50	By writing the sums as: $1 + 999, 2 + 998, 3 + 997, \dots, 499 + 501, 500 + 500$ . It is clear that the number of different pairs is five hundred.
51	<p>Considering the number of 1's used in the sum.</p> <p>6x1's: <math>1+1+1+1+1+1</math>  5x1's: None  4x1's: <math>1+1+1+1+2</math>  3x1's: <math>1+1+1+3</math>  2x1's: <math>1+1+2+2</math> and <math>1+1+4</math>  1x1: <math>1+2+3</math> and <math>1+5</math>  0x1's: <math>2+2+2, 2+4</math> and <math>1+3</math></p> <p>Giving 10 solutions.</p>
52	Let us consider the first and second digit. Changing the first digit, ?9 10 numbers (i.e. 09, 19, 29, ... , 99). Changing the second digit, 9? 10 numbers (i.e. 90, 91, 92, ... , 99). Making a total of 20 number nines being written.
53	Gurmit paid \$2, \$4, \$6, \$1 and \$8 for the five presents.
54	There are 3 Zids with 4 spots and 4 Zods with 9 spots.
56	Nasreen bought 4 angel fish and 8 goldfish.
59	$(3/10)*? = 24$ and $24/(3/10) = 80$ . Aunt Helen is 80 years old.
60	<p>Write the ages as (A), (A + 2), (A + 4), (A + 6).</p> <p><math>4A + 12 = 28</math>  <math>4A = 16</math>  <math>A = 16/4 = 4</math></p>

	Youngest sister is ( A ) = 4. ( 4 )+( 6 )+( 8 )+( 10 )=28
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SAMPLE